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## Chapter 2. Teaching for the Application of Concepts and Thinking Skills

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**Note From the Publisher**: The authors have provided video and web content throughout the book that is available to you through QR (quick response) codes. To read a QR code, you must have a smartphone or tablet with a camera. We recommend that you download a QR code reader app that is made specifically for your phone or tablet brand.



Videos may also be accessed at resources.corwin.com/vlmathematics-k-2